

# 3D shapes reconstruction based on 2D views

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## Contents

<b>1</b>	<b>Neural Network approach for shape from shading problem</b>	<b>3</b>
1.1	The objective	3
1.2	Defining the illumination model	3
1.2.1	The diffuse model	4
1.2.2	The specular model	6
1.2.3	Hybrid model	7
1.3	Using neural networks	7
1.3.1	The FNN	7
1.3.2	The RBF	7
1.4	Putting all together	7
1.4.1	The learning algorithm	7
<b>2</b>	<b>Interpolation approach</b>	<b>8</b>
<b>3</b>	<b>Hybrid solution</b>	<b>9</b>
<b>A</b>	<b>Listing of PMC library</b>	<b>11</b>
A.1	pmc_macro.hh	11
A.2	pmc_datatypes.hh	11
A.3	pmc_activation.hh	12
A.4	pmc_activation.hxx	13
A.5	pmc_neuron.hh	15
A.6	pmc_neuron.hxx	16
A.7	pmc_neuron.cc	17
A.8	pmc_layer.hh	19
A.9	pmc_layer.hxx	20
A.10	pmc_layer.cc	20
A.11	pmc_network.hh	22
A.12	pmc_network.hxx	23
A.13	pmc_network.cc	24
A.14	test.cc	27
	<b>Bibliography</b>	<b>29</b>

### Abstract

The aim of this paper is to study possibilities of 3D objects construction from 2D views using neural networks. The goal isn't to apply directly this paper in an industrial context. We do not have all constraint than in real application. It study specular approach based on one view and interpolation method and it try to find a solution.

**Keywords:** neural networks, shape from shading.

## Introduction

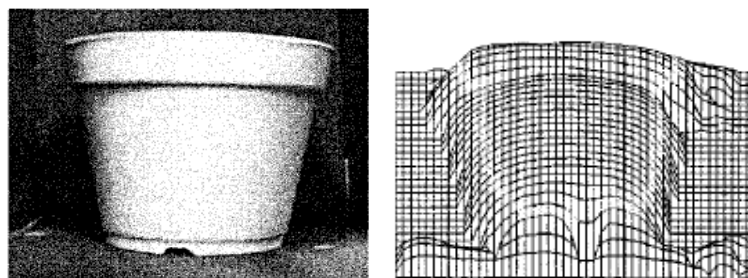
The variation in brightness due to change in surface orientation across a surface can be used to extract shape of object. Extracting 3D shape information from one or multiple 2D shading images<sup>1</sup> has been one the classic research problems in low-level vision. In this paper, we try to use neural networks to solve problem. We studied two approachs: specular base model and interpolation model.

## 1 Neural Network approach for shape from shading problem

To reconstruct a 3D shape, you can use the shading information. The method **Shape From Shading**, or SFS, is the one explained below. The shading is **the brightness variation** from one point of an image to one of its neighbors[2].

### 1.1 The objective

The aim is to recover spatial information from a picture:



### 1.2 Defining the illumination model

The first thing needed is the illumination model. A lot of model exists like:

- ambient illumination model
- diffuse illumination model

---

<sup>1</sup>As know as the shape from shading problem

- specular illumination model
- ...

and a choice must be made.

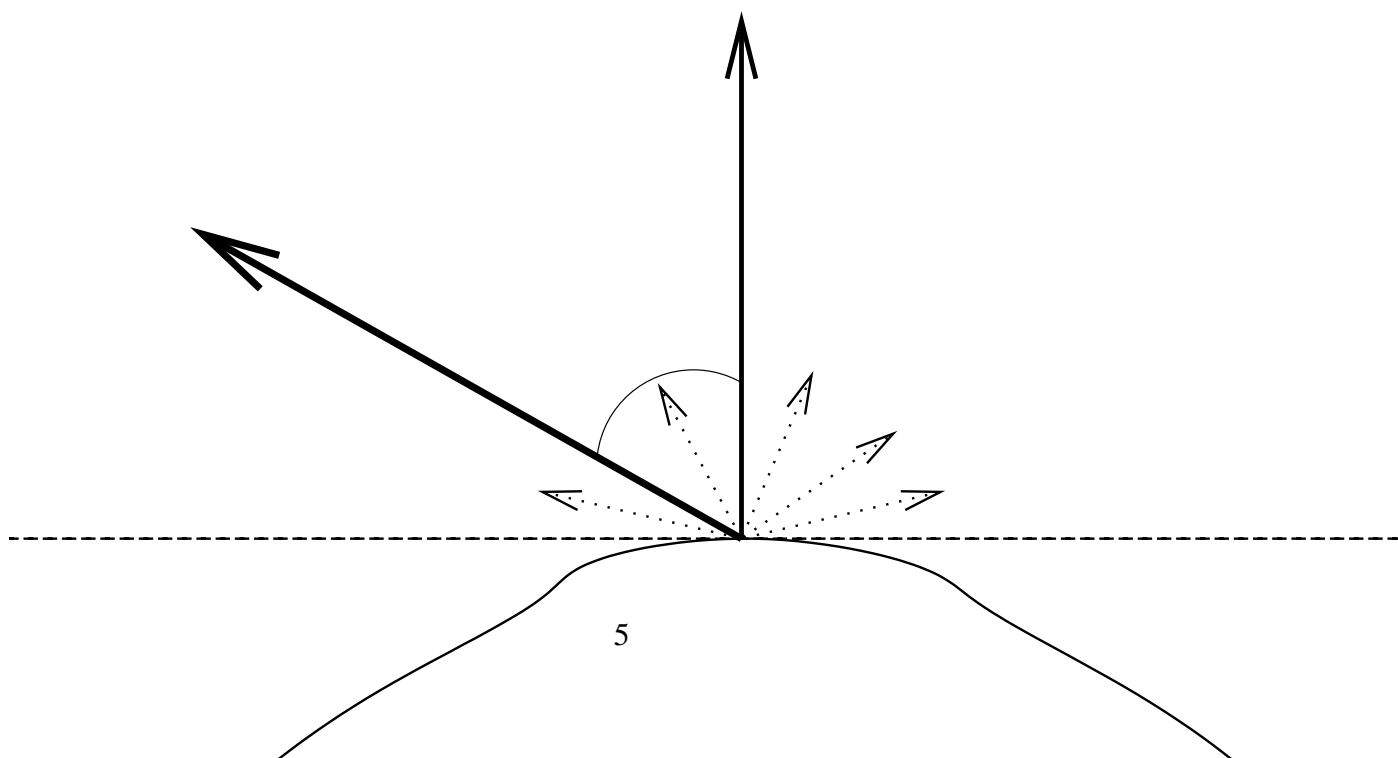
All these models can be combined to have a more realistic yet simple model.

### 1.2.1 The diffuse model

The most known diffuse model is the Lambert<sup>2</sup> model suppose that when a light heat a surface, the reflected light depends only on the angle between the light direction and the surface normal, and that the light is **equally** reflected in all direction.

---

<sup>2</sup>Johann Heinrich Lambert (26/08/1728 - 25/09/1777), has published is Photometria in 1760, the Lambertian diffuse lighting model.



The following formula is used in 2D:

$$R_{diffuse} = \eta \cdot \vec{N} \cdot \vec{L}$$

where  $\left\| \begin{array}{l} \eta \\ \vec{N} \\ \vec{L} \end{array} \right\|$  the albedo of the surface (measure of reflectivity)  
 surface normal  
 light source direction

In 3D, the formula becomes:

$$R_{diffuse}(p(x,y), q(x,y)) = \eta(n \cdot s^t), \forall(x,y)$$

with  $\left\| \begin{array}{l} \eta \\ n \\ s^t = \begin{pmatrix} \cos\tau \\ \sin\sigma \cdot \sin\tau \\ \sin\sigma \cdot \cos\sigma \end{pmatrix} \\ p(x,y) = \frac{\partial z}{\partial x} \\ q(x,y) = \frac{\partial z}{\partial y} \end{array} \right\|$  the albedo  
 the normal norm  
 light source direction  
 the depth variation on the x axis (surface gradient)  
 the depth variation on the y axis

In order to use it this model, the light source direction must be known, and this is not always the case.

### 1.2.2 The specular model

In addition to diffuse, there is the specular reflection model.

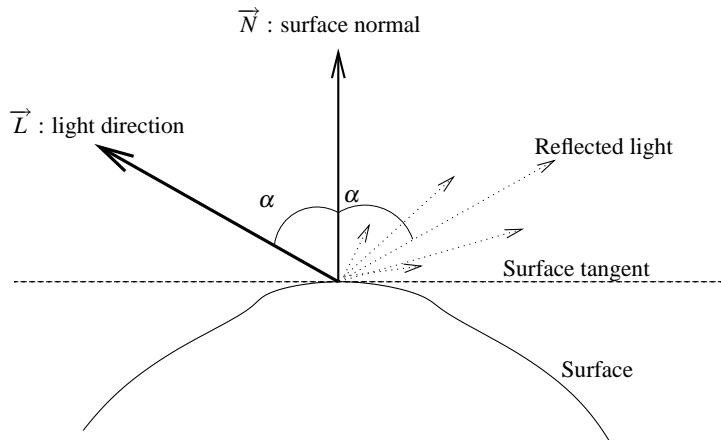


Figure 2: The specular model

This model does not work well for reality picture, but there is a better model derived from that one.

### 1.2.3 Hybrid model

Since none of the previous model is enough, an hybrid model is defined. It's a simple addition with a coefficient:

$$R_{hybrid} = (1 - w) \cdot R_{diffuse} + w \cdot R_{specular}$$

## 1.3 Using neural networks

Now that the illumination model is defined, the next step is to define how to use neural networks capabilities in the model.

### 1.3.1 The FNN

Based on the universal approximation of FNN (Forward Neural Network), a proper function  $F_{FNN}$  is defined as the diffuse component of the Lambertian model:

$$\begin{aligned} R_{diffuse}(p, q) &= F_{FNN}(a) \\ &= \varphi_a \left( v_0 + \sum_{k=1}^N v_k \cdot \varphi_a(w_k \cdot a_{i,j}) \right) \end{aligned}$$

where  $\begin{cases} w_k & \text{weights vector connected between the input and the hidden layer} \\ v_k \text{ and } v_0 & \text{weights and the bias connected between hidden layer and the output layer} \\ N & \text{number of hidden unit} \end{cases}$

### 1.3.2 The RBF

RBFs are well designed for nonlinear separable problem and use a bell-shape Gaussian activation function.

## 1.4 Putting all together

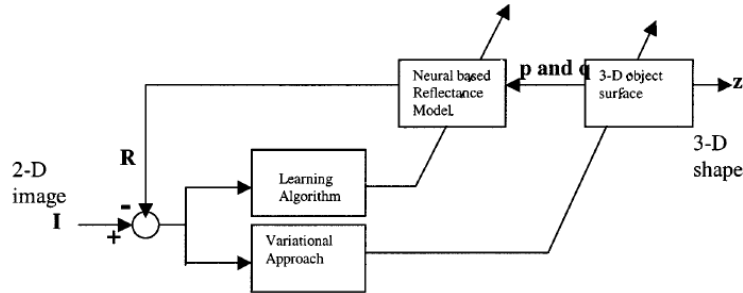


Figure 3: The hybrid neural network model

### 1.4.1 The learning algorithm

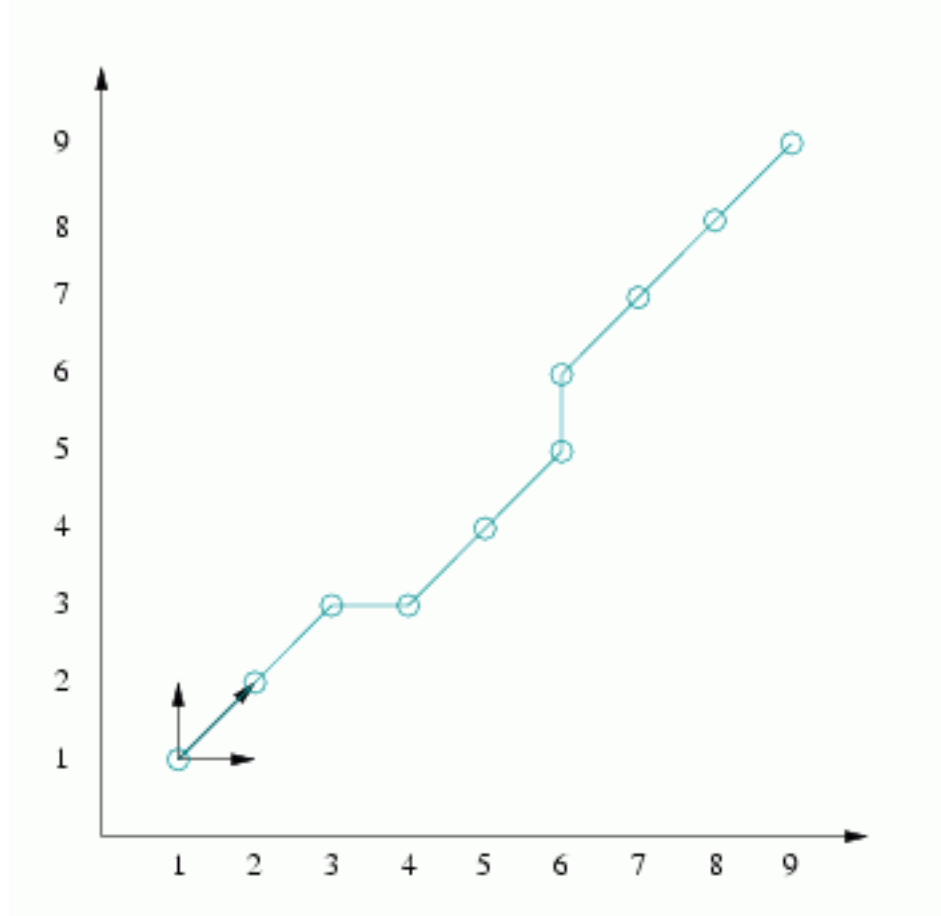
1.  $n_i = 0$

2. The surface gradient  $p_{i,j}$  and  $q_{i,j}$ , and the depth  $z_{i,j}$  receive 0.
3. The weights of the NN are randomly initialized
4. while the stop criterion is not meet do:
  - (a)  $n \leftarrow n + 1$
  - (b) for each  $(i, j)$  do
    - i. Calculate  $\frac{\partial R_{NN}(a_{i,j})}{\partial p}$  and  $\frac{\partial R_{NN}(a_{i,j})}{\partial q}$
    - ii. Estimate  $p_{i,j}(n)$  and  $q_{i,j}(n)$
    - iii. Estimate  $z_{i,j}(n)$
    - iv. Compute the free parameters
    - v. Find the error between  $I_{i,j}$  and  $R_{NN}(a_{i,j})$

## 2 Interpolation approach

Koch[8][7][6] studied reconstruction of 3D scenes from uncalibrated image sequences. His works has interested us because he have good results and they are applied in creation of 3D map of Sagalassos archaeological excavation site. First, his method try to interpolate the different views. To do this, it use dynamic programing. His algorithm is near DTW algorithm. It try to connect each point between views warping views.

Figure 4: Illustration of minimization of distance between to 1D view using dynamic programming. Each axes represent 1D view. We try to connect each point between two views.



Next, it estimate depth of point using stereo matching algorithms. Knowing camera position, it's easy to found depth of point. Finally, it refine estimation using the different viewpoints.

Koch has good results with this approach. Nevertheless, it do not use neural networks.

### 3 Hybrid solution

Specular approach use only one view of object. We want use informations given by series of views.

Interpolation approach use some characteristics of views we do not want to use and its approach don't use neuronal networks.

We try to make a solution using specular approach of [2] and interpolation approach of [6]. But this work is not yet finished

## **Conclusion**

It should now find a method to use specular model using picture interpolation. we have not got time to solve it and problem stay open.

Our work is far to be finish. Our solution is only theoretical. This paper is not completed without results, but we hope it could be used as pedagogical aims. We have add in appendices our perceptron implementation used for our tests.

## A Listing of PMC library

### A.1 pmc\_macro.hh

```

#ifndef MACRO_HH
# define MACRO_HH

#ifdef FORALL
#undef FORALL
#endif // !FORALL

# define FORALL(Type, Container, Ite) \
    for (Type::iterator Ite = Container.begin(); \
         Ite != Container.end(); \
         ++Ite)

#ifdef CFORALL
#undef CFORALL
#endif // !FORALL

# define CFORALL(Type, Container, Ite) \
    for (Type::const_iterator Ite = Container.begin(); \
         Ite != Container.end(); \
         ++Ite)

#endif

```

### A.2 pmc\_datatypes.hh

```

#ifndef PMC_DATA_TYPES_HH
# define PMC_DATA_TYPES_HH

#include <iostream>
#include <vector>
#include "pmc_macro.hh"

namespace pmc
{

    class Neuron;
    class Layer;
    class Network;

    typedef double                data_type;
    typedef std::vector<data_type> datas_type;

    typedef Layer                layer_type;
    typedef std::vector<layer_type *> layers_type;
    typedef std::vector<unsigned int> desc_layers_type;

    typedef Neuron               neuron_type;
    typedef std::vector<neuron_type *> neurons_type;

    typedef double                weight_type;
    typedef std::vector<weight_type> weights_type;

    inline std::ostream& operator<<(std::ostream &ostr, const datas_type &v)
    {
        CFORALL(pmc::datas_type, v, i)
            ostr << (*i) << " ";
        return ostr;
    }
}

```

```

}
} // namespace pmc

```

```
#endif // !PMC_DATA_TYPES_HH
```

```
#define BIAIS 1.0
```

### A.3 pmc\_activation.hh

```
#ifndef PMC_ACTIVATION_HH
# define PMC_ACTIVATION_HH
```

```
# include "pmc_datatypes.hh"
```

```
namespace pmc
```

```
{
  class ActivationFunc
  {
  public:
    ActivationFunc(const std::string &name);
    virtual ~ActivationFunc();
    virtual data_type normal(data_type in, double theta) const = 0;
    virtual data_type derivate(data_type in, double theta) const = 0;
    inline std::ostream &print(std::ostream &ostr) const;
  protected:
    const std::string name_;
  };

  // \f f_{act} (x, \Theta) = \tanh (x - \Theta) \f
  class AFTanh : public ActivationFunc
  {
  public:
    inline AFTanh::AFTanh();
    inline data_type normal(data_type in, double theta) const;
    inline data_type derivate(data_type in, double theta) const;
  };

  /// \f f_{act} (x, \Theta) = \frac{1}{1 + e^{-(x - \Theta)}} \f
  class AFLog : public ActivationFunc
  {
  public:
    inline AFLog::AFLog();
    inline virtual data_type normal(data_type in, double theta) const;
    inline virtual data_type derivate(data_type in, double theta) const;
  };

  /// \f f_{act} (x, \Theta) = x - \Theta \f
  class AFLinear : public ActivationFunc
  {
  public:
    inline AFLinear::AFLinear();
    inline data_type normal(data_type in, double theta) const;
    inline data_type derivate(data_type in, double theta) const;
  };

  /** \f f_{act} (x, \Theta) = \left\{ \begin{array}{cl} 1.0 & x \geq \\ \Theta & -1.0 & x < \Theta \end{array} \right. \f
  */
  class AFBinary : public ActivationFunc
  {

```

```

public:
    inline AFBinary::AFBinary();
    inline data_type normal(data_type in, double theta) const;
    inline data_type derivate(data_type in, double theta) const;
};

/** \f f_{act} (x, \Theta) = 3(AFLog.normal(x, \Theta) - 1/2) \f
 */
class AFLogNormalized : public AFLog
{
public:
    inline AFLogNormalized::AFLogNormalized();
    inline data_type normal(data_type in, double theta) const;
    inline data_type derivate(data_type in, double theta) const;
};

inline std::ostream& operator<< (std::ostream &ostr,
                                const ActivationFunc &func);

} // namespace pmc

# include "pmc_activation.hxx"
#endif // ! PMC_ACTIVATION_HH

```

## A.4 pmc\_activation.hxx

```

namespace pmc
{
    inline ActivationFunc::ActivationFunc(const std::string &name) : name_(name)
    {
    }

    inline ActivationFunc::~~ActivationFunc()
    {
    }

    inline std::ostream &ActivationFunc::print(std::ostream &ostr) const
    {
        ostr << name_;
        return ostr;
    }

    // Tanh

    inline AFTanh::AFTanh() : ActivationFunc("tanh")
    {
    }

    inline data_type AFTanh::normal(data_type in, double theta) const
    {
        return (tanh (in - theta));
    }

    inline data_type AFTanh::derivate(data_type in, double theta) const
    {
        return (1.0 - pow (tanh (in - theta), 2.0));
    }

    // Log

```

```

inline AFLog::AFLog() : ActivationFunc("log")
{
}

inline data_type AFLog::normal(data_type in, double theta) const
{
    return (1.0 / (1.0 + pow (M_E, theta - in)));
}

inline data_type AFLog::derivate(data_type in, double theta) const
{
    double      e_val;

    e_val = pow (M_E, theta - in);

    return (e_val / pow (e_val + 1.0, 2.0));
}

// Normalized Log

inline AFLogNormalized::AFLogNormalized() : AFLog()
{
}

inline data_type AFLogNormalized::normal(data_type in, double theta) const
{
    return 3.0 * (AFLog::normal(in, theta) - 0.5);
}

inline data_type AFLogNormalized::derivate(data_type in, double theta) const
{
    return 0.75 - (pow(normal(in, theta), 2) / 3);
}

// Linear

inline AFLinear::AFLinear() : ActivationFunc("linear")
{
}

inline data_type AFLinear::normal(data_type in, double theta) const
{
    return (in - theta);
}

inline data_type AFLinear::derivate(data_type in, double theta) const
{
    return (1.0);
}

// Binary

inline AFBinary::AFBinary() : ActivationFunc("linear")
{
}

inline data_type AFBinary::normal(data_type in, double theta) const
{
    if (in >= theta)
        return (1.0);
}

```

```

    return (-1.0);
}

inline data_type AFBinary::derivate(data_type in, double theta) const
{
    return (1.0);
}

inline std::ostream& operator<< (std::ostream &ostr,
                                const ActivationFunc &func)
{
    return func.print(ostr);
}
} // namespace pmc

```

## A.5 pmc\_neuron.hh

```

#ifndef PMC_NEURON_HH
#define PMC_NEURON_HH

#include <vector>
#include <iostream>
#include "pmc_datatypes.hh"
#include "pmc_activation.hh"

namespace pmc
{
    class Neuron
    {
    public:
        Neuron(unsigned int id, unsigned int nb_weights,
              const ActivationFunc *phi);
        ~Neuron();

        std::istream      &load(std::istream &istr);
        std::ostream      &print(std::ostream &ostr) const;
        inline std::ostream &save(std::ostream &ostr) const;

        data_type         operator()(const data_type &in);

        void              deltaEval(const neurons_type &succ);
        void              deltaEval(data_type optimal, double tolerance);
        inline void       deltaSet(double delta);
        inline double     deltaGet() const;

        inline void       thetaSet(double theta);
        inline double     thetaGet() const;

        inline double     weightGet(unsigned int i) const;
        void              weightsUpdate(double epsilon);
        void              weightsModifReset();
        void              weightsModifEval(const neurons_type &prev,
                                         bool stochastic);
        void              weightsModifEval(const data_type &in,
                                         bool stochastic);

        inline void       activationFunctionSet(const ActivationFunc *phi);

        inline data_type  inputGet() const;
    };
}

```

```

    inline data_type    outputGet() const;

private:
    unsigned int        id_;
    weights_type        weights_;
    weights_type        weights_diff_;

    const ActivationFunc *phi_;

    data_type           input_;
    data_type           output_;

    double              delta_;
    double              theta_;
};

inline std::istream& operator>> (std::istream &istr, Neuron &neuron);
inline std::ostream& operator<< (std::ostream &ostr, const Neuron &neuron);

} // namespace pmc

#include "pmc_neuron.hxx"

#endif // !PMC_NERON_HH

```

## A.6 pmc\_neuron.hxx

```

#include "pmc_neuron.hh"

namespace pmc
{
    inline void    Neuron::activationFunctionSet(const ActivationFunc *phi)
    {
        phi_ = phi;
    }

    inline void    Neuron::deltaSet(double delta)
    {
        delta_ = delta;
    }

    inline double Neuron::deltaGet() const
    {
        return delta_;
    }

    inline void    Neuron::thetaSet(double theta)
    {
        theta_ = theta;
    }

    inline double Neuron::thetaGet() const
    {
        return theta_;
    }

    inline double Neuron::inputGet() const
    {
        return input_;
    }
}

```

```

inline double Neuron::outputGet() const
{
    return output_;
}

inline std::ostream &Neuron::save(std::ostream &ostr) const
{
    return print(ostr);
}

inline double Neuron::weightGet(unsigned int i) const
{
    return weights_[i];
}

inline std::istream& operator>> (std::istream &istr, Neuron &neuron)
{
    return neuron.load(istr);
}

inline std::ostream& operator<< (std::ostream &ostr, const Neuron &neuron)
{
    return neuron.print(ostr);
}

} // namespace pmc

```

## A.7 pmc\_neuron.cc

```

#include <cassert>
#include "pmc_macro.hh"
#include "pmc_neuron.hh"

namespace pmc
{
    Neuron::Neuron(unsigned int id, unsigned int nb_weights,
                  const ActivationFunc *phi)
        : id_(id), weights_(nb_weights, 1), weights_diff_(nb_weights, 0.0),
          phi_(phi), delta_(rand() / (double) RAND_MAX - 0.5), theta_(0)
    {
        for (weights_type::iterator w = weights_.begin();
             w != weights_.end(); ++w) {
            *w = rand() / (double) RAND_MAX - 0.5;
        }
    }

    Neuron::~Neuron()
    {
    }

    std::istream &Neuron::load(std::istream &istr)
    {
        FORALL(weights_type, weights_, i)
            istr >> *i;
        return istr;
    }

    std::ostream &Neuron::print(std::ostream &ostr) const
    {
        ostr << "delta= " << delta_ << "\t|";
        weights_type::const_iterator wdiff = weights_diff_.begin();
    }
}

```

```

    CFORALL(weights_type, weights_, i)
        ostr << " " << *i << " (" << *(wdiff++) << ")";
    ostr << " |";
    return ostr;
}

data_type      Neuron::operator()(const datas_type &in)
{
    input_ = 0;

    datas_type::const_iterator v = in.begin();
    CFORALL(weights_type, weights_, w)
        input_ += (*w) * *(v++);
    output_ = phi_->normal(input_, theta_);
    return output_;
}

void Neuron::deltaEval(const neurons_type &succ)
{
    delta_ = 0.0;
    CFORALL(neurons_type, succ, i)
        delta_ += (*i)->weightGet(id_) * (*i)->deltaGet();
    delta_ *= phi_->derivate(input_, theta_);
}

void Neuron::deltaEval(data_type optimal, double tolerance)
{
    data_type diff = output_ - optimal;

    delta_ = phi_->derivate(input_, theta_);
    if ((tolerance != 0.0) && (diff >= (-1.0 * tolerance)) &&
        (diff <= tolerance))
        diff = 0.0;
    delta_ *= diff;
}

void Neuron::weightsModifEval(const neurons_type &prev, bool stochastic)
{
    weights_type::iterator wdiff = weights_diff_.begin();

    CFORALL(neurons_type, prev, p)
        if (stochastic)
            *(wdiff++) = (*p)->outputGet() * delta_;
        else
            *(wdiff++) += (*p)->outputGet() * delta_;
}

void Neuron::weightsModifEval(const datas_type &in, bool stochastic)
{
    weights_type::iterator wdiff = weights_diff_.begin();
    CFORALL(datas_type, in, i)
        if (stochastic)
            *(wdiff++) = (*i) * delta_;
        else
            *(wdiff++) += (*i) * delta_;
}

void Neuron::weightsUpdate(double epsilon)
{
    weights_type::const_iterator wdiff = weights_diff_.begin();
    FORALL(weights_type, weights_, w)
        *w = *w - epsilon * *(wdiff++);
}

```

```

}

void Neuron::weightsModifReset()
{
    FORALL(weights_type, weights_diff_, w)
        *w = 0.0;
}

} // namespace pmc

```

## A.8 pmc\_layer.hh

```

#ifndef PMC_LAYER_HH
#define PMC_LAYER_HH

#include <vector>
#include <iostream>
#include "pmc_datatypes.hh"
#include "pmc_neuron.hh"
#include "pmc_activation.hh"

namespace pmc
{

class Layer
{
public:
    Layer(unsigned int size, unsigned int previous_size,
          const ActivationFunc *phi);
    ~Layer();

    std::istream &load(std::istream &istr);
    std::ostream &print(std::ostream &ostr) const;
    std::ostream &save(std::ostream &ostr) const;

    inline unsigned int size() const;
    inline const neurons_type &neuronsGet() const;

    void operator()(const datas_type &in, datas_type &out);

    void deltasEval(Layer &succ);
    void deltasEval(const datas_type &optimal, double tolerance);
    void deltasReset();
    void postprocess(Layer &succ, double epsilon, bool stochastic);
    void postprocess(const datas_type &in, double epsilon,
                    bool stochastic);
    void weightsUpdate(double epsilon);
    void weightsModifReset();

    inline void activationFunctionSet(const ActivationFunc *phi);

private:
    neurons_type neurons_;
};

inline std::istream& operator>> (std::istream &istr, Layer &layer);
inline std::ostream& operator<< (std::ostream &ostr, const Layer &layer);

} // namespace pmc

#include "pmc_layer.hxx"

```

```
#endif // ! PMC_LAYER_HH
```

## A.9 pmc\_layer.hxx

```
#include "pmc_layer.hh"

namespace pmc
{

    inline void Layer::activationFunctionSet(const ActivationFunc *phi)
    {
        FORALL(neurons_type, neurons_, i)
            (*i)->activationFunctionSet(phi);
    }

    inline void Layer::deltasReset()
    {
        FORALL(neurons_type, neurons_, i)
            (*i)->deltaSet(0.0);
    }

    inline unsigned int Layer::size() const
    {
        return neurons_.size();
    }

    inline const neurons_type &Layer::neuronsGet() const
    {
        return neurons_;
    }

    inline std::istream& operator>> (std::istream &istr, Layer &layer)
    {
        return layer.load(istr);
    }

    inline std::ostream& operator<< (std::ostream &ostr, const Layer &layer)
    {
        return layer.print(ostr);
    }

} // namespace pmc
```

## A.10 pmc\_layer.cc

```
#include <cassert>
#include "pmc_macro.hh"
#include "pmc_layer.hh"

namespace pmc
{

Layer::Layer(unsigned int size, unsigned int previous_size,
             const ActivationFunc *phi)
    : neurons_(size)
{
    unsigned int id = 0;
    FORALL(neurons_type, neurons_, i)
        (*i) = new neuron_type(id++, previous_size, phi);
}

}
```

```

Layer::~Layer()
{
    FORALL(neurons_type, neurons_, i)
        delete (*i);
}

std::istream &Layer::load(std::istream &istr)
{
    FORALL(neurons_type, neurons_, i)
        istr >> **i;
    return istr;
}

std::ostream &Layer::print(std::ostream &ostr) const
{
    unsigned int id = 0;
    CFORALL(neurons_type, neurons_, i)
        ostr << " w" << id++ << ": " << **i << std::endl;
    return ostr;
}

std::ostream &Layer::save(std::ostream &ostr) const
{
    CFORALL(neurons_type, neurons_, i)
        ostr << **i << std::endl;
    ostr << std::endl;
    return ostr;
}

void Layer::operator()(const datas_type &in, datas_type &out)
{
    out.clear();
    CFORALL(neurons_type, neurons_, i)
    {
        //Biases
        data_type t = BIAIS;
        if (i != neurons_.begin())
            t = (**i)(in);
        out.push_back(t);
    }
}

void Layer::deltasEval(Layer &succ)
{
    neurons_type successors = succ.neuronsGet();
    FORALL(neurons_type, neurons_, i)
        //Biases
        if (i != neurons_.begin())
            (*i)->deltaEval(successors);
}

void Layer::deltasEval(const datas_type &optimal, double tolerance)
{
    assert(neurons_.size() == optimal.size() + 1);
    datas_type::const_iterator o = optimal.begin();

    FORALL(neurons_type, neurons_, i)
        //Biases
        if (i != neurons_.begin())
            (*i)->deltaEval(*(o++), tolerance);
}

void Layer::postprocess(Layer &prev, double epsilon, bool stochastic)
{

```

```

neurons_type prevNeurons = prev.neuronsGet();
FORALL(neurons_type, neurons_, i)
    // Biases
    if (i != neurons_.begin())
        (*i)->weightsModifEval(prevNeurons, stochastic);
}

void Layer::postprocess(const datas_type &in, double epsilon,
                       bool stochastic)
{
    FORALL(neurons_type, neurons_, i)
        //Biases
        if (i != neurons_.begin())
            (*i)->weightsModifEval(in, stochastic);
}

void Layer::weightsUpdate(double epsilon)
{
    FORALL(neurons_type, neurons_, i)
        //Biases
        if (i != neurons_.begin())
            (*i)->weightsUpdate(epsilon);
}

void Layer::weightsModifReset()
{
    FORALL(neurons_type, neurons_, i)
        //Biases
        if (i != neurons_.begin())
            (*i)->weightsModifReset();
}
} // namespace pmc

```

## A.11 pmc\_network.hh

```

#ifndef PMC_NETWORK_HH
#define PMC_NETWORK_HH

#include <vector>
#include "pmc_layer.hh"
#include "pmc_activation.hh"
#include "pmc_datatypes.hh"

namespace pmc
{
class Network
{
public:
    Network(unsigned int input_size, unsigned int output_size,
            desc_layers_type layers, double epsilon,
            const ActivationFunc *phi);
    Network(const char *filename, double epsilon, const ActivationFunc *phi);
    ~Network();

    inline std::istream &load(std::istream &istr);
    inline std::ostream &print(std::ostream &ostr) const;
    std::ostream &save(std::ostream &ostr) const;

    const datas_type &operator()(const datas_type &in);

    void weightsUpdate();

```

```

void          weightsModifReset();

void          learn(const datas_type &in,
                  const datas_type &optimal,
                  bool stochastic,
                  double tolerance = 0);

// FIXME: Not yet the good formula.
double        errorGet(const datas_type &optimal) const;

inline void    activationFunctionSet(const ActivationFunc *phi);

private:
void          layersInit_(desc_layers_type &layers,
                        const ActivationFunc *phi);
inline void    deltasReset_();

void          backpropagate_(const datas_type &optimal, double tolerance);
void          postprocess_(bool stochastic);

private:

layers_type    *layers_;

unsigned int    input_size_;
unsigned int    output_size_;
double          epsilon_;

datas_type      output_;
datas_type      input_;

};

inline std::istream& operator>> (std::istream &istr, pmc::Network &net);
inline std::ostream& operator<< (std::ostream &ostr, const pmc::Network &net);

} // namespace pmc

#include "pmc_network.hxx"

#endif /* !PMC_NETWORK */

```

## A.12 pmc\_network.hxx

```

#include <cassert>
#include "pmc_network.hh"

namespace pmc
{
    inline void Network::activationFunctionSet(const ActivationFunc *phi)
    {
        FORALL(layers_type, (*layers_), i)
            (*i)->activationFunctionSet(phi);
    }

    inline void Network::deltasReset_()
    {
        FORALL(layers_type, (*layers_), i)
            (*i)->deltasReset();
    }
}

```

```

inline std::istream &Network::load(std::istream &istr)
{
    FORALL(layers_type, (*layers_), i)
        istr >> **i;
    return istr;
}

inline std::ostream &Network::print(std::ostream &ostr) const
{
    unsigned int id = 0;
    CFORALL(layers_type, (*layers_), i)
    {
        ostr << "Layer " << id++ << std::endl;
        ostr << **i;
    }
    return ostr;
}

inline std::istream& operator>> (std::istream &istr, pmc::Network &net)
{
    return net.load(istr);
}

inline std::ostream& operator<< (std::ostream &ostr, const pmc::Network &net)
{
    return net.print(ostr);
}

} // namespace pmc

```

## A.13 pmc\_network.cc

```

#include <cassert>
#include <vector>
#include <fstream>
#include "pmc_macro.hh"
#include "pmc_network.hh"

namespace pmc
{
    Network::Network(unsigned int input_size, unsigned int output_size,
                     desc_layers_type layers, double epsilon,
                     const ActivationFunc *phi)
        : input_size_(input_size), output_size_(output_size),
          epsilon_(epsilon)
    {
        assert(input_size_);
        assert(output_size_);

        // Je ne suis pas d'accord avec cet assert, on peut avoir un PMC sans
        // couche intermediaire
        //assert(layers.size());

        //biais
        input_size_++;
        output_size_++;
        FORALL(desc_layers_type, layers, i)
            (*i)++;

        layers.push_back(output_size_);
        layersInit_(layers, phi);
    }
}

```

```

    assert(layers_);
}

Network::Network(const char *filename, double epsilon,
                const ActivationFunc *phi)
: input_size_(0), output_size_(0), epsilon_(epsilon)
{
    std::ifstream file(filename);

    try
    {
        // Read number of layers.
        unsigned int layers = 0;
        file >> layers;
        if (layers < 2)
            throw 1;

        // Read input size.
        file >> input_size_;
        if (!input_size_)
            throw 2;

        // Read each layer size.
        desc_layers_type sizes(layers - 2);
        FORALL(desc_layers_type, sizes, i)
        {
            if (!file.good())
                throw 3;
            file >> *i;
        }

        // Read output size.
        file >> output_size_;
        if (!output_size_)
            throw 4;
        sizes.push_back(output_size_);

        // Build Network.
        layersInit_(sizes, phi);
        load(file);
    }
    catch(...)
    {
        file.close();
        std::cerr << "Network (loader): Error while loading file: '"
                  << filename << "'" << std::endl;
        exit(0);
    }
}

void Network::layersInit_(desc_layers_type &layers, const ActivationFunc *phi)
{
    layers_ = new layers_type(layers.size());
    layers_type::iterator l = layers_->begin();

    std::cout << "layers : " << layers[0] << std::endl;
    unsigned int previous_size = input_size_;

    CFORALL(desc_layers_type, layers, i)
    {
        std::cout << "previous : " << previous_size << std::endl;
        *(l++) = new layer_type(*i, previous_size, phi);
    }
}

```

```

        previous_size = *i;
    }
}

Network::~Network()
{
    if (layers_)
    {
        FORALL(layers_type, (*layers_), i)
            delete *i;
        delete layers_;
    }
}

std::ostream &Network::save(std::ostream &ostr) const
{
    ostr << layers_->size() + 1 << "\n"
          << input_size_ << " ";
    CFORALL(layers_type, (*layers_), i)
        ostr << (*i)->size() << " ";
    ostr << "\n" << std::endl;
    CFORALL(layers_type, (*layers_), i)
        (*i)->save(ostr);
    return ostr;
}

const datas_type &Network::operator()(const datas_type & in)
{
    assert(in.size()+1 == input_size_);

    input_ = in;
    input_.insert(input_.begin(), BIAIS);
    datas_type input = input_;

    CFORALL(layers_type, (*layers_), i)
    {
        (**i)(input, output_);
        input = output_;
    }
    assert(output_.size() == output_size_);
    // Virer le Biais
    output_.erase(output_.begin());
    return output_;
}

void Network::backpropagate_(const datas_type &optimal, double tolerance)
{
    assert(optimal.size()+1 == output_size_);

    layers_type::reverse_iterator i(layers_->end());
    layers_type::reverse_iterator end(layers_->begin());

    layer_type *succ = 0;

    (*i)->deltasEval(optimal, tolerance);
    for (succ = *(i++); i != end; succ = *(i++))
        (*i)->deltasEval(*succ);
}

void Network::postprocess_(bool stochastic)
{
    layer_type *prev = 0;

```

```

FORALL(layers_type, (*layers_), i)
{
    if (prev == 0)
        (*i)->postprocess(input_, epsilon_, stochastic);
    else
        (*i)->postprocess(*prev, epsilon_, stochastic);
    prev = (*i);
}
}

void Network::weightsUpdate()
{
    FORALL(layers_type, (*layers_), i)
        (*i)->weightsUpdate(epsilon_);
}

void Network::weightsModifReset()
{
    FORALL(layers_type, (*layers_), i)
        (*i)->weightsModifReset();
}

double Network::errorGet(const datas_type &optimal) const
{
    double error = 0;
    datas_type::const_iterator j = output_.begin();
    CFORALL(datas_type, optimal, i)
    {
        error += ((*j) - (*i)) * ((*j) - (*i));
        ++j;
    }
    return error;
}

void Network::learn(const datas_type &in, const datas_type &optimal,
                    bool stochastic, double tolerance)
{
    this->operator()(in);
    // std::cout << "in: " << in[0] << ", " << in[1] << std::endl;
    // std::cout << "out : " << output_[0] << ", " << output_[1] << std::endl;
    // std::cout << "optimal : " << optimal[0] << ", " << optimal[1] << std::endl;
    backpropagate_(optimal, tolerance);
    postprocess_(stochastic);
}
} // namespace pmc

```

## A.14 test.cc

```

#include "pmc_datatypes.hh"
#include "pmc_network.hh"
#include "pmc_activation.hh"

using namespace pmc;

int main()
{
    pmc::AFLog f;
    pmc::Network net("sample.in", 0.2, &f);
    std::cout << net << std::endl;
    //net.save(std::cout);
}

```

```
pmc::datas_type in;
in.push_back(-1);
in.push_back(1);
pmc::datas_type ref;
ref.push_back(0.2);
ref.push_back(0.7);

std::cout << net(in) << std::endl;

for (unsigned int i = 0; i < 1000; ++i)
    net.learn(in, ref, 0);

std::cout << net << std::endl;
std::cout << net(in) << std::endl;

return 0;
}
```

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